INDEX								
	GATE PYQs – PHYSICAL CHEMISTRY							
CHAPTER NO.	CHAPTER NAME	PAGE NO.						
1	STRUCTURE & QUANTUM CHEMISTRY	1						
2	GROUP THEORY	25						
3	MOLECULAR SPECTROSCOPY	32						
4	EQUILIBRIUM	43						
	Unit-1: Chemical Thermodynamics	43						
	Unit-2: Chemical Equilibrium	61						
•	Unit-3: Electrochemistry	64						
•	Unit-4: Phase Equilibrium	75						
	Unit-5: Statistical Thermodynamics	88						
5	KINETICS	93						
6	SURFACES AND INTERFACES	109						
	GATE PYQs – INORGANIC CHEMISTRY							
CHAPTER NO.	CHAPTER NAME	PAGE NO.						
1	MAIN GROUP ELEMENT	114						
2	TRANSITION ELEMENTS	125						
3	LANTHANIDE AND ACTINIDE	152						
4	ORGANOMETALICS	159						
5	RADIOACTIVITY	179						
6	BIOINORGANIC	180						
7	SOLIDS	187						
8	INSTRUMENTAL METHOD OF ANALYSIS	194						
	GATE PYQs – ORGANIC CHEMISTRY							
CHAPTER NO.	CHAPTER NAME	PAGE NO.						
1	STEREOCHEMISTRY	198						
2	REACTION MECHANISMS	224						
3	REACTIVE INTERMEDIATES	248						
4	ORGANIC SYNTHESIS – REAGENTS	287						
5	PERICYCLIC REACTIONS & PHOTOCHEMISTRY	319						
6	HETEROCYCLIC COMPOUNDS	348						
7	BIOMOLECULES	359						
8	EXPERIMENTAL TECHNIQUES IN ORGANIC CHEMISTRY	367						

# SECTION - I

# "PHYSICAL CHEMISTRY"

NUMBER OF QU	SER OF	: QUE	STIO	JESTIONS ASKED IN GATE EXAM (2000 - 2025)	KED	N GA	VIE 13	XAM	(2000	) - 20	25)				
Units	2025	2024	2023	2022	2021	2020	2019	2018	2017	2016	2015	2014	2013	2012	2011
Structure : Quantum Chemistry	7	2	4	5	3	3	4	9	9	3	3	3	4	2	3
Group Theory	2	3	2	1	1	1	1	ı	ı	1	ı	1	П	Н	1
Molecular Spectroscopy	1	2	1	4	4	4	1	3		2	1	1	1	2	2
Equilibrium : 1. Chemical Thermodynamics	2	3	1	1	3	3	2	2	2	2	9	4	2	3	ı
2. Chemical Equilibrium	ı	1	ı	ı	2	ı	1	ı	ı	1	ı	1	1	1	ı
3. Electrochemistry	1	2	2	1	2	2	1	3	3	1	4	1	3	П	2
4. Phase Equilibrium	2	2	2	1	3	1	2	1	1	1	1	1	1	2	3
5. Statistical Thermodynamics	3	-	1	2	-	-	2	1	1	1	1	2	1	1	
Kinetics	2	3	4	3	2	4	2	3	5	4	2	1	3	2	4
Surfaces and Interfaces	-	1	2	1	_	1	2	1	1	1	1	1	1	-	-
Units	2010	2009	2008	2007	2006	2005	2004	2003	2002	2001	2000				
Structure : Quantum Chemistry	3	7	1	5	9	7	3	1	5	3	1				
Group Theory	1	2	2	-	7	-	2	-	1	1	-				
Molecular Spectroscopy	2	2	9	3	1	2	3	2	5	3	1				
Equilibrium : 1. Chemical Thermodynamics	5	4	4	3	9	5	6	7	3	8	4				
2. Chemical Equilibrium	1	•	-	_	1	-	2	1	_	2	1				
3. Electrochemistry	1	1	1	4	2	3	1	4	3	3	1				
4. Phase Equilibrium	3	3	1	2	4	5	4	2	4	-	3				
5. Statistical Thermodynamics	_	-	1	2	1	-	-	2	-	-	-				
Kinetics	1	2	3	7	3	3	5	5	3	-	2				
Surfaces and Interfaces	1		1	-	1	1	•	1	-	-	1				

# STRUCTURE & QUANTUM CHEMISTRY

### **Previous Year Exam Question & Solutions**

[GATE 2000]

1. ${}^{2}P_{3/3}$	is	the	ground	state	of
--------------------	----	-----	--------	-------	----

(a) H

(b) Li

(c) B

(d) F

[GATE 2001]

2. As per the uncertainty principle,  $\Delta x \cdot \Delta py =$ 

(a) *h* 

(b)  $h / 2\pi$ 

(c)  $\lambda$ 

(d) zero

[GATE 2001]

3. The second lower state of particle in a cubic box is

- (a) non degenerate
  - (b) doubly degenerate
  - (c) triply degenerate
  - (d) six-fold degenerate

[GATE 2001]

4. Given than,  $\Psi_{n,l,m}$   $(r,\theta,\varphi) = R_{n,l}$  (r)  $(\theta,\varphi)$ ;  $R_{20}$  (r)  $\alpha$   $(2-r/a_0)$   $e^{-r/a_0}$ ,  $Y_{0,0}$   $(\theta,\varphi) = 1/\sqrt{4\pi}$ . The position of radial node in the 2s orbital is at

(a)  $r = a_0$ 

(b)  $r = 2a_0$ 

(c)  $r = a_0 / 2$ 

(d)  $r = a_0 / 4$ 

[GATE 2002]

5. The ground state of aluminium atom is

(a)  ${}^{2}P_{1/2}$ 

(b)  ${}^{2}P_{3/2}$ 

(c)  ${}^4P_{5/2}$ 

(d)  ${}^{4}P_{3/2}$ 

[GATE 2002]

6. The velocity of the electron in the hydrogen atom

- (a) increases with increasing principal quantum number
- (b) decreases with increasing principal quantum number
- (c) is uniform for any value of the principal quantum number
- (d) first increases and then decreases with principal quantum number

[GATE 2002]

7. In allene, hybridization of the central and terminal carbons respectively are

(a)  $sp^2$  and  $sp^2$ 

(b)  $sp^2$  and  $sp^3$ 

(c) sp and  $sp^2$ 

(d) sp and  $sp^3$ 

[GATE 2002]

8. The probability of finding a free particle inside the left half of a 1-dimensional box of length L is

(a) L/2

(b)  $\sqrt{(2/L)}$ 

(c) 2/L

(d) 1/2

### [GATE 2002]

9. The force between two electrons separated by 0.1 nm in vacuum ( $\varepsilon_0=8.854\times 10^{-12}J^{-2}C^{-2}m^{-1}$ ) is

(a)  $2.31 \times 10^{-8}$ N

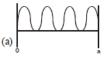
(b)  $-2.31 \times 10^{-8}$  N

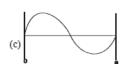
(c)  $-1.15 \times 10^{-8}$  N

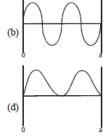
(d) 1.155 x 10<sup>-8</sup>N

### [GATE 2003]

 For the energy level (2h²/ma²) the probability for a particle of mass 'm' over the length 'a' of a one-dimensional box is depicted by







[GATE 2004]

11. In units of  $\frac{h^2}{8m^2}$ , the energy difference between levels corresponding to 3 and 2 node eigenfunctions for a particles of mass in a one dimensional box of length  $\ell$  is

(a) 1

(b) 3

(c) 5

(d) 7

[GATE 2004]

12. On the basis o LCAO-MO theory, the magnetic characteristics of  $N_2$  and  $N_2^+$  are

- (a) both diamagnetic
- (b) both paramagnetic
- (c)  $N_2$  dimagnetic and  $N_2^+$  paramagnetic
- (d)  $N_2$  paramegnetic and  $N_2^+$  diamagnetic

[GATE 2004]

13. Match the following:

P. 4n+2 rule	I. Woodward-Hoffmann ruleII.
Q. single valued	II. Bound system
R. <p>=0</p>	III. Hurtree-Fock Theory
S. photochemically allowed	IV. Huckeltheory
	V. Wave function
	VI. unbound system

Codes:

(a) P-I. Q-III, R-IV, S-VI

(b) P-II, Q-VI, R-III, S-I

(c) P-IV, Q-V, R-II, S-VI

(d) P-IV, Q-V, R-II, S-I

### [GATE 2005]

- 14. The set of eigenfunctions  $\sqrt{\frac{2}{a}}\sin\frac{n\pi x}{a}$   $(0 \le a, n = 1, 2, 3...)$ 
  - (a) orthogonal
  - (b) normalized
  - (c) both orthogonal and normalized
  - (d) unnormalized

### [GATE 2005]

- 15. The function  $e^{ax^2}(\alpha > 0)$  is not an acceptable wave function for bound system, because
  - (a) it is not continuous
- (b) it is multivalued
- (c) it is not normalisable
- (d) all of these

### [GATE 2005]

- 16. First order perturbation correction  $\Delta \epsilon_n^{(1)}$  to energy level  $\epsilon_n$  of a simple harmonic oscillator due to the anharmonicity perturbation  $\gamma x^3$  is given b.
  - (a)  $\Delta \varepsilon_n^{(1)} = \gamma$
- (b)  $\Delta \varepsilon_n^{(1)} = \gamma^2$
- (c)  $\Delta \varepsilon_n^{(1)} = \gamma^{-1}$
- (d)  $\Delta \varepsilon_n^{(1)} = 0$

### [GATE 2005]

- 17. The 2s orbital of H-atom has radial node at  $2a_0$  because  $\Psi_{2s}$  is proportional to
  - (a)  $\left(\frac{1}{2} + \frac{r}{a_0}\right)$
- (b)  $\left(2 + \frac{r}{a_0}\right)$
- (c)  $\left(2-\frac{r}{a}\right)$
- (d)  $\left(2-\frac{r}{2a_0}\right)$

### **IGATE 2005**

- 18. The orbital  $\Psi=\,1_{S_{H_A}}-1_{S_{H_B}} \text{of water belongs to the}$  irreducible representation
  - (a) A<sub>1</sub>

(b) B<sub>1</sub>

(c) A<sub>2</sub>

(d) B<sub>2</sub>

### [GATE 2005]

- 19. As per Huckel theory,  $\pi$ --electron energy levels of cyclobutadiene are
  - (a)  $\alpha + 2\beta$ ,  $\alpha + \beta$ ,  $\alpha \beta$ ,  $\alpha + 2\beta$ ,
  - (b)  $\alpha$  + 2 $\beta$ ,  $\alpha$   $\beta$ ,  $\alpha$   $\beta$ ,  $\alpha$  2 $\beta$ ,
  - (c)  $\alpha$  + 2 $\beta$ ,  $\alpha$ ,  $\alpha$ ,  $\alpha$  2 $\beta$ ,
  - (d)  $\alpha + \beta$ ,  $\alpha \beta$ ,  $\alpha \beta$ ,  $\alpha 2\beta$ ,

### [GATE 2005]

- 20. Given  $\beta = -75$  kJ/mol,
  - (a) paramagnetic and its lowest absorption energy is 150 kl
  - (b) paramagnetic and its lowest absorption energy is 75 kJ
  - (c) diamagnetic and its lowest absorption energy is 75 kJ
  - (d) diamagnetic and its lowest absorption energy is 150 kJ.

### [GATE 2006]

- 21. In the Huckel model for benzene, the  $\pi$  electronic transitions from the occupied to the unoccupied molecular orbitals do NOT occur at
  - (a) 4B

(b) 3β

(c)  $2\beta$ 

(d) 1β

### [GATE 2006]

22. To demonstrate the variational principle, a trial function  $\psi = C_1 + \frac{\Psi_{2s} + \Psi_{3s}}{\sqrt{2}} + C_2 + \frac{\Psi_{2s} + \Psi_{3s}}{\sqrt{2}} \text{ where } C_1 \text{ and } C_2 \text{ are the variational parameters and} \\ \psi_{2s} \psi_{3s} \text{ and are the 2s, and 3s orbitals of the hydrogen atom, is constructed. The corresponding secular determinant for the hydrogen atom (in eV) is$ 

(a) 
$$\begin{vmatrix} 3.4\left(1+\frac{4}{9}\right)2 - E & 3.4(1-4/9)/2\\ 3.4(1-4/9)/2 & 3.4\left(1+\frac{4}{9}\right)2 - E \end{vmatrix}$$

(b) 
$$\begin{vmatrix} 3.4\left(1+\frac{4}{9}\right)2 - E & 3.4(1-4/9)/2 \\ 3.4(1-4/9)/2 & 3.4\left(1-\frac{4}{9}\right)2 - E \end{vmatrix}$$

(c) 
$$\begin{vmatrix} 3.4\left(1+\frac{4}{9}\right)2 - E & 3.4(1+4/9)/2 \\ 3.4(1-4/9)/2 & 3.4\left(1-\frac{4}{9}\right)2 - E \end{vmatrix}$$

(d) 
$$\begin{vmatrix} 3.4\left(1+\frac{4}{9}\right)2-E & 0\\ 0 & 3.4\left(1+\frac{4}{9}\right)2-E \end{vmatrix}$$

### [GATE 2006]

- 23. Which of the following pairs of operators commute?
  - (a) x and d/dx
- (b) d/dx and  $d^2/dx^2 + 2d/dx$
- (c)  $x^2d/dx$  and  $d^2/dx^2$
- (d)  $x^2$  and d/dx

### [GATE 2006]

- 24. The zero-point energy of the vibration of  $^{35}\text{Cl}_2$  mimicking a harmonic oscillator with a force constant k = 2293.8 Nm $^{-1}$  is
  - (a)  $10.5 \times 10^{-21} \, \text{J}$
- (b)  $14.8 \times 10^{-21} \, \text{J}$
- (c)  $20 \times 10^{-21}$  J
- (d)  $29.6 \times 10^{-21} \text{ J}$

### [GATE 2006]

- 25. The first excited state wavefunction for a particle in a box that spans from –a to +a is
  - (a)  $\sqrt{\frac{1}{a}}\cos\left(\frac{\pi x}{a}\right)$
- (b)  $\sqrt{\frac{1}{a}} sin\left(\frac{\pi x}{a}\right)$
- (c)  $\sqrt{\frac{2}{a}}\cos\left(\frac{2\pi x}{a}\right)$
- (d)  $\sqrt{\frac{2}{a}} sin\left(\frac{2\pi x}{a}\right)$

### [GATE 2006]

- 26. A perturbation  $V=\delta(x-a/2)$  is introduced in the box. The first order energy correction to the first excited state is
  - (a) 0

(b) 2/a

(c) 1/a

(d) 1/2a

### [GATE 2007]

- 27. For a homonuclear diatomic molecule, the bonding molecular orbital is
  - (a)  $\sigma_u$  of lowest energy
  - (b)  $\sigma_u$  of second lowest energy
  - (c)  $\pi_q$  of lowest energy
  - (d)  $\pi_u$  oflowest energy

### [GATE 2007]

- 28. The ionisation potential of hydrogen atom is 13.6 eV. The first ionisation potential of a sodium atom, assuming that the energy of its outer electron can be represented by a H-atom like model with an effective nuclear charge of 1.84, is
  - (a) 46.0 Ev

(b) 11.5 eV

(c) 5.1 eV

(d) 2.9 eV

### [GATE 2007]

- 29. The quantum state of a particle moving in a circular path in a plane is given by  $\Psi_m(\phi) = \left(\frac{1}{\sqrt{2\pi}}\right)e^{im\phi}$ , m = O, ±1, ±2, .... When a perturbation H<sub>1</sub>= P cos ¢ is applied (P is a constant), what will be the first order correction to the energy of Ihem<sup>th</sup> state
  - (a) 0

(b)  $P/(2\pi)$ 

- (c) P/(4 $\pi$ )
- (d)  $Pm^2/(4\pi^2)$

### [GATE 2007]

- 30. Consider a particle of mass m moving in a one-dimensional box under the potential V=0 for  $0 \le x \le a$  and  $V = \infty$  outside the box. When the partial is in its lowest energy state the average momentum ( $\langle p_x \rangle$ ) of the particle is
  - (a)  $< p_x > = 0$
- (b)  $< p_x >= h/a$
- (c)  $< p_x >= h/2a$
- (d)  $< p_x > = h/2\pi a$

### [GATE 2007]

- 31. The uncertainty in the momentum ( $\Delta px$ ) of the particle in its lowest energy state is
  - (a)  $\Delta p_x = 0$

- (b)  $\Delta p_x = h/a$
- (c)  $\Delta p_x = h/2a$
- (d)  $\Delta p_x = h/2\pi a$

### [GATE 2008]

- 32. The wave function of a diatomic molecule has the form =  $0.89~\varphi_{covalent} + 0.45~\varphi_{ionic}$ . The chance that both electrons of the bond will be found on the same atom in 100 inspections of the molecule approximately is
  - (a) 79

(b) 20

(c) 45

(d) 60

### [GATE 2009]

- 33. The minimum number of electrons needed to form a chemical bond between two atoms is
  - (a) 1

(b) 2

(c) 3

(d) 4

### [GATE 2009]

- 34. The ground state electronic energy (Hartree) of a helium atom, neglecting the inter-electron repulsion, is
  - (a) 1.0

(b) - 0.5

(c) - 2.0

(d) - 4.0

### [GATE 2009]

- 35. A particle is confined to a one-dimensional box of length 1 mm. If the length is changed by 10<sup>-9</sup> the % change in the ground state energy is
  - (a) 2 x 10<sup>-4</sup>

(b) 2 x 10<sup>-7</sup>

- (c)  $2 \times 10^{-2}$
- (d) 0

### [GATE 2009]

- 36. The operation of the commutator [x, d/dx] on a function f(x) is equal to
  - (a) 0

(b) f(x)

(c) - f(x)

(d) x df/dx

### [GATE 2009]

- 37. The lowest allowed energy is equal to zero for
  - (a) the hydrogen atom
  - (b) a rigid rotor
  - (c) a harmonic oscillator
  - (d) a particle in a 3-dimensional box

### [GATE 2009]

- 38. The degeneracy of a quantum particle in a cubic box having energy four times that of the lowest energy is
  - (a) 3

(b) 6

(c) 1

(d) 4

### [GATE 2009]

- 39. The de Broglie wavelength for a He atom travelling at 1000  $\,$  ms  $^{\!-1}$  (typical speed at room temperature) is
  - (a) 99.7 x 10<sup>-12</sup> m
- (b) 199.4 x 10<sup>-12</sup> m
- (c) 199.4 x 10<sup>-18</sup> m
- (d) 99 x 10<sup>-6</sup> m

### [GATE 2010]

40. For eigen functions  $\Psi_1 = \sqrt{\frac{1}{b} sin\left(\frac{\pi x}{b}\right)}$  and  $\Psi_2 =$ 

$$\sqrt{\frac{2}{b}} \sin\left(\frac{2\pi x}{b}\right)$$
 of particle in a 1-D box of length b(0  $\leq x \leq$ b)

- (a)  $\Psi_1$  is normalized and orthogonal to  $\Psi_2$
- (b)  $\Psi_1$  is normalized but not orthogonal to  $\Psi_2$
- (c)  $\Psi_2$  is nonnalized and orthogonal  $\Psi_1$
- (d)  $\Psi_2$  is neither normalized nor orthogonal to  $\Psi_1$

### [GATE 2010]

- 41. The commutator  $[x^3, p_x]$  is equal to
  - (a)- $\frac{3hx^2}{2\pi i}$

(b)  $\frac{hx}{2\pi}$ 

(c)  $\frac{hx^2}{2\pi i}$ 

(d)  $\frac{3hx^2}{2\pi i}$ 

### [GATE 2010]

- 42. An electron of mass 'm' is confined to a one dimensional box of length. 'b'. If it makes a radiative transition from second excited state to the ground state. The frequency of the photon emitted is
  - (a) 9h/8mb<sup>2</sup>
- (b) 3h/8mb<sup>2</sup>
- (c)  $h/mb^2$

(d)  $2h/mb^2$ 

### [GATE 2011]

- 43. The wave function for a Harmonic oscillator described by  $N x \exp(-ax^2/2)$  has
  - (a) one maximum only
  - (b) one maximum, one minimum only
  - (c) two maxima, one minimum only
  - (d) two maxima, two minima only

### [GATE 2011]

- 44. If an arbitrary wave function is used to calculate the energy of a quantum mechanical system, the value calculated is never less than the true energy. The above statement relates to
  - (a) perturbation theory
  - (b) variation principle
  - (c) Heisenberg's uncertainty principle
  - (d) quantization of energy

### [GATE 2011]

- 45. The wave function for a quantum mechanical particle in a 1-dimensional box of length 'a' is given by  $\Psi = A \sin \frac{\pi x}{a}$ . The value of 'A' for a box of length 200 nm is
  - (a)  $4 \times 10^4 \text{ (nm)}^2$
- (b)  $10\sqrt{2} \text{ (nm)}^{1/2}$
- (c)  $\sqrt{2} / 10 \text{ (nm)}^{-1/2}$
- (d) 0.1 (nm)<sup>-1/2</sup>

### [GATE 2012]

- 46. Let  $\phi_x^{\mathcal{C}}$  and  $\phi_z^{\mathcal{C}}$  denote the wavefunctions of the 2px and 2pz orbitals of carbon, respectively, and  $\phi_x^0$  and  $\phi_z^0$  represent the wavefunctions of the 2px and 2pz orbitals of oxygen, respectively. If C<sub>1</sub> and C<sub>2</sub>are constants used in linear combinations and the CO molecule is oriented along the z axis, then, according to molecular orbital theory, the  $\pi$ -bonding molecular orbital has a wavefunction given by
  - (a)  $C_1 \phi_z^C + C_2 \phi_x^O$
- (b)  $C_1 \phi_z^C + C_2 \phi_z^O$
- (c)  $C_1 \phi_x^C + C_2 \phi_z^O$
- (d)  $C_1 \phi_x^C + C_2 \phi_x^O$

### [GATE 2012]

47. The wavefunction of a 1-D harmonic oscillator between x =  $+\infty$  and x =  $-\infty$ is given by  $\Psi$  (x) = N (2x<sup>2</sup> -1) $e^{-x^2/2}$ . The value of N that normalizes the function  $\Psi$  (x) is (Given:

$$\int_{-\infty}^{+\infty} x^{2n} e^{-x^2} dx = \frac{1 \cdot 3 \cdot 5 \dots (2n-1)}{2^n} \sqrt{\pi}$$

- (b)  $\left(\frac{1}{3\sqrt{\pi}}\right)^{1/2}$  (d)  $\left(\frac{1}{4\sqrt{\pi}}\right)^{1/2}$

Statement for Linked Answer Questions 48 and 49: Hückel molecular orbital theory can be applied to the allene radical. CH<sub>2</sub>=CH-CH<sub>2</sub>

### [GATE 2012]

48. The secular determinant (where  $\alpha$ ,  $\beta$  and E have their usual meanings) is given by

(a) 
$$\begin{vmatrix} \alpha - E & \beta & 0 \\ \beta & \alpha - E & \beta \\ 0 & \beta & \alpha - E \end{vmatrix}$$
(b) 
$$\begin{vmatrix} \alpha - E & 0 & 0 \\ 0 & \alpha - E & \beta \\ 0 & \beta & \alpha - E \end{vmatrix}$$
(c) 
$$\begin{vmatrix} \alpha - E & \beta & 0 \\ \beta & \alpha - E & 0 \\ 0 & 0 & \alpha - E \end{vmatrix}$$
(d) 
$$\begin{vmatrix} \alpha - E & -\beta & 0 \\ -\beta & \alpha - E & -\beta & 0 \\ -\beta & \alpha - E & -\beta & 0 \\ -\beta & \alpha - E & -\beta & 0 \end{vmatrix}$$

- 49. The possible values of E are
  - (a)  $\alpha + \sqrt{2\beta}$ ,  $\alpha$ ,  $\alpha \sqrt{2\beta}$
- (b)  $\alpha + \sqrt{2\beta}$ ,  $\alpha$ ,  $\alpha \sqrt{2\beta}$
- (c)  $\alpha + \beta$ ,  $\alpha$ ,  $\alpha \beta$
- (d)  $\alpha + 2\beta$ ,  $\alpha$ ,  $\alpha 2\beta$

### [GATE 2012]

- 50. If  $\Delta y$  and  $\Delta p_y$  are the uncertainties in the y-coordinate and the y component of the momentum of a particle respectively, then, according to principle $\Delta y \Delta p_y$  is  $(\hbar = \frac{h}{2\pi}$  and h is Planck's constant)
  - (a) ≥  $\hbar$

(b)  $>\hbar/2$ 

(c) >ħ

 $(d) \geq \hbar/2$ 

### [GATE 2013]

- 51. Two trial wave functions  $\phi_1 = c_1 x(a-x)$  and  $\phi_2 = c_1 x(a-x) + c_2 x(a-x)$  $c_1x^2(a-x)^2$  give ground state energies  $E_1$  and  $E_2$ , respectively, for the microscopic particle in a 1-D boxby using the variation method. If the exact ground state energy is E<sub>0</sub>, the correct relationship between E<sub>0</sub>, E<sub>1</sub> and E<sub>2</sub>
  - (a)  $E_0 = E_1 = E_2$
- (b)  $E_0 < E_1 < E_2$
- (c)  $E_0 < E_2 < E_1$
- (d)  $E_0 > E_2 = E_1$

### [GATE 2013]

52. The ground state energies of H atom and H<sub>2</sub> molecule are -13.6 eV and -31.7 eV, respectively. The dissociation energy of H<sub>2</sub> is \_\_\_\_\_ eV.

- 53.  $e^{-2x^2}$  is an eigen function of the operator  $\left(\frac{d^2}{dx^2} 16x^2\right)$ . The corresponding eigen value is

  - (a) + 4

(b) - 4

(c) + 2

(d) - 2

### [GATE 2013]

- 54. The angular part of the wavefunction for the electron in a hydrogen atom is proportional to  $\sin^2\theta$  cos  $\theta e^{2i\phi}$ . The values of the azimuthal quantum number ( I ) and the magnetic quantum number (m) are, respectively
  - (a) 2 and 2
- (b) 2 and -2

- (c) 3 and 2
- (d) 3 and -2

### [GATE 2014]

- 55. The value of the magnetic quantum number of a  $p_x$  orbital
  - (a) 1

(b) 0

(c) +1

(d) undefined

### [GATE 2014]

- 56.  $\psi = N r (6 Z r) e^{-Zr/3} \cos \theta$ , is a proposed hydrogenic wavefunction, where Z= Atomic number, r= radial distance from the nucleus,  $\theta =$  azimuthal angle, N is a constant. The INCORRECT statement about  $\psi$  is
  - (a)  $\psi = 0$  in the xy-plane
  - (b) two radial nodes are present in  $\psi$
  - (c) one angular node is present in  $\psi$
  - (d) the size of the orbital decreases with increase in atomic number

### [GATE 2025]

- 106. If a particle's state function is an eigenfunction of the operator  $\hat{L}^2$  with eigenvalue  $30\hbar^2$ , then the possible eigenvalue(s) of the operator  $\hat{L}^2z$  for the same state function is/are
  - (a) 10ħ²

(b) 16ħ²

(c) 25ħ²

(d) 0

				Ansv	wer Key				
1	2	3	4	5	6	7	8	9	10
d	d	С	b	а	b	а	d	а	a
11	12	13	14	15	16	17	18	19	20
d	С	d	С	С	d	С	d	С	a
21	22	23	24	25	26	27	28	29	30
d	a	b	b	b	С	d	С	a	a
31	32	33	34	35	36	37	38	39	40
С	b	a	d	a	b	b	С	а	С
41	42	43	44	45	46	47	48	49	50
а	С	b	b	d	d	С	а	a	d
51	52	53	54	55	56	57	58	59	60
С	4.4 to 4.6	b	С	d	b	a	d	а	896 to 900
61	62	63	64	65	66	67	68	69	70
d	b	b	b	а	899 to 901	225 to 240	33.30 to 36.90	0.80 to 0.84	a
71	72	73	74	75	76	77	78	79	80
С	4.4 to 4.6	a	0.55 to 0.65	210 to 216	С	0.5	0	2.8 to 3.0	b
81	82	83	84	85	86	87	88	89	90
С	a	c,d	2000	39.5 to 40.5	d	5	b,d	0.18 to 0.20	2
91	92	93	94	95	96	97	98	99	100
С	a	b	a	2	С	b,c	3	8	74.10 to 74.30
101	102	103	104	105	106				
3.110 to 3.200	b	b, c	С	а, с	b, c, d				

### Solutions

### 1. Solution: Correct answer is (d).

 ${}^{2}P_{3/2}$  is the ground state for p<sup>5</sup> systems, i.e. systems with one unpaired electron and more than half – filled p orbitals.

H and Li are s<sup>1</sup> systems, B is a p<sup>3</sup> system, while F is a p<sup>5</sup> system.

### 2. Solution: Correct answer is (d).

The uncertainty principle applied to uncertainties in the same direction. Hence, if the uncertainties in x and  $p_y$  are in two different directions, then the product of the uncertainties is zero.

### 3. Solution: Correct answer is (c).

The second lowest energy state of a particle in a cubic box has quantum numbers

$$(n_x, n_y, n_z) = (1,1,2), (1,2,1), (2,1,1)$$

All of these states have energy

$$E^{3D} = (1^2 + 1^2 + 2^2) \frac{h^2}{8ma^2} = 6 \frac{h^2}{8ma^2}$$

Hence, the second lowest state has degeneracy = 3.

### 4. Solution: Correct answer is (b).

The value of r where the radial part of the wave function becomes zero is the radial node. The given radial part is

$$R_{20}(r) \propto \left(2 - \frac{r}{a_0}\right) e^{-r/a_0}$$

This can be zero only if

$$\left(2 - \frac{r}{a_0}\right) = 0$$

$$r = 2a_0$$

Hence, correct answer is (B).

### 5. **Solution:** Correct answer is (a).

Aluminium has electronic configuration  $1s^2\ 2s^2\ 2p^6\ 3s^2\ 3p^1$ , i.e. aluminium is a  $p^1$  system. The ground state term symbol will have L=1, i.e. Term Symbol P and S=+1/2. Thus, spin multiplicity will be 2S+1=2.

Also the J values range from (L + S) to |L - S|.

$$\therefore J = \frac{3}{2}, \frac{1}{2}$$

As the system is less than half-filled, the lowest J value has lower energy.

Hence, the ground state term symbol is  ${}^{2}P_{1/2}$ .

### 6. Solution: Correct answer is (b).

According to Bohr's theory,

$$v = \frac{n\hbar}{mr}$$

and

$$r = \frac{n^2}{Z} \times a_0$$

$$\therefore v = \frac{Z\hbar}{ma_0} \times \frac{1}{n}$$

$$\therefore v \propto \frac{1}{n}$$

Thus, at higher quantum numbers, velocity is lower.

### 7. **Solution:** Correct answer is a.

Structure of allene is



It can be clearly seen that all carbons have a planar geometry, and hence, are  $sp^2$  hybridized.

### 8. Solution: Correct answer is (d).

The probability of a free particle in a one – dimensional box is symmetric about the center of the box. Hence, the probabilities in the left half and the right half are equal. As the total probability is one, the probability in the left half will be 1/2.

### 9. Solution: Correct answer is (a).

According to the Coulomb's law,

$$\begin{split} F &= \frac{q_1 q_2}{4\pi \varepsilon_0 r^2} \\ &= \frac{(-1.6 \times 10^{-19}) \times (-1.6 \times 10^{-19})}{4 \times \pi \times 8.854 \times 10^{-12} \times (0.1 \times 10^{-9})^2} \\ &= 2.3 \times 10^{-8} \ N \end{split}$$

### 10. Solution: Correct answer is (a).

$$E_n = \frac{n^2 h^2}{8ma^2} = \frac{2h^2}{ma^2}$$
$$\therefore \frac{n^2}{8} = 2$$
$$\therefore n = 4$$

For this energy level, number of nodes= n - 1 = 3.

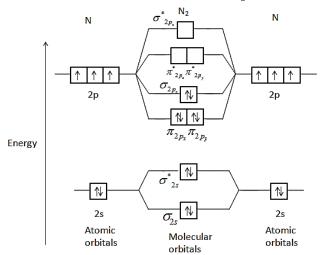
Also, probabilty density functions will always be positive, i.e. above the X – axis. Hence, (B) and (C) cannot be the answers. Also, (C) has only one node.

### 11. Solution: Correct answer is (d).

For a particle in a one – dimensional box, if number of nodes is 2, then quantum number n=3, and if number of nodes is 3, then quantum number n=4.

### 12. Solution: Correct answer is (c).

The LCAO – MO energy level diagram for  $N_2$  is



As there are no unpaired electrons,  $N_2$  is diamagnetic. However, during formation of  $N_2^+$ , an electron from  $\sigma_- 2p_z$  will be removed, thus, resulting in an unpaired electron. Hence,  $N_2^+$  is paramagnetic.

### 13. Solution: Correct answer is (d).

The Huckel theory gives the (4n + 2) electron rule for aromaticity.

For a wavefunction to be acceptable, it must be single valued

The average value of momentum, <P>, is zero for bound systems.

The Woodward – Hoffmann rules give the photochemically allowed transitions.

### 14. Solution: Correct answer is (c).

The given set of eigenfunctions is eigenfunctions of a one dimensional box. According to the theorems of Quantum Mechanics, the eigenfunctions of a given system form an orthonormal set. Hence, the given eigenfunctions are both orthogonal and normalized.

The set of eigen function is  $\sqrt{\frac{2}{a}} \sin \frac{n\pi x}{a}$ 

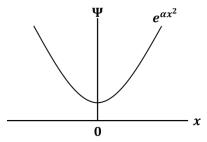
is normalized.

$$\int_{0}^{a} \sqrt{\frac{2}{a}} \sin \frac{n\pi x}{a} \sqrt{\frac{2}{a}} \sin \frac{n\pi x}{a} dx = 1 \rightarrow normalized if n$$

$$= 1$$

$$\int_{0}^{a} \sqrt{\frac{2}{a}} \sin \frac{\pi x}{a} \sqrt{\frac{2}{a}} \sin \frac{2\pi x}{a} dx = 0 \rightarrow orthogonal$$

### 15. Solution: Correct answer is (c).



For a wavefunction to be acceptable, it MUST (a) be continuous, (b) be single valued, (c) be finite (normalisable) and (d) have a continuous derivative. As can be seen in the graph, the function  $e^{\alpha x^2}$  is continuous, single-valued, and has a continuous derivative, but is NOT finite (NOT normalisable).

### 16. **Solution:** Correct answer is (d).

For a simple harmonic oscillator, an odd perturbation function results in the first order energy correction being zero.

i.e. 
$$\Delta \varepsilon_n^{(1)} = 0$$
.

### 17. Solution: Correct answer is (c).

If a radial nodes exists at  $r=2a_0$ , it means that  $r-2a_0=0$ .

If we divide by  $a_0$  on both sides, we get

$$\frac{r}{a_0} - 2 = 0 \ OR \ \left(2 - \frac{r}{a_0}\right) = 0$$

Thus, a radial node will exist at  $r=2a_{0}$  if the wavefunction

$$\Psi_{2s} \propto 2 - \frac{r}{a_0}$$

### 18. Solution: Correct answer is d.

The given molecular orbital will lose the rotational  $\hat{\mathcal{C}}_2$  and the reflection  $\hat{\sigma}_v$  (perpendicular plane) symmetries, but the identity  $(\hat{E})$  and  $\hat{\sigma}_v{}'$  (molecular plane) symmetries will be intact. Hence, this orbital will transform according to the  $B_2$  symmetry of the  $C_{2v}$  point group.



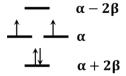
### 19. Solution: Correct answer is (c).

The  $\pi$  – electron energy level diagram of cyclobutadiene, according to the Huckel theory, is given by

$$\begin{array}{ccc}
 & \alpha - 2\beta \\
 & \uparrow & \alpha \\
 & \downarrow & \alpha + 2\beta
\end{array}$$

### 20. **Solution:** Correct answer is (a).

The  $\pi$  – electron energy level diagram of cyclobutadiene, according to the Huckel theory, is given by

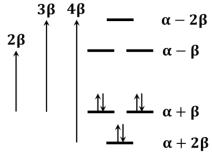


It can be seen that there are two  $\pi$  – electrons. Hence, cyclobutadiene is paramagnetic.

Also, the lowest absorption energy is given by

$$\Delta E = (\alpha - 2\beta) - \alpha = -2\beta$$
  
= (-2) × (-75) = 150 kJ mol<sup>-1</sup>

### 21. Solution: Correct answer is (D).



According to Huckel model for benzene, the energy level diagram is as shown in the figure. The six  $\pi$  electrons are arranges in the two lowest levels. Thus, it can be seen from the diagram that the  $\pi$  electronic transitions from the occupied to the unoccupied levels will have energy  $2\beta$ ,  $3\beta$  and  $4\beta$ .

As a transition with energy  $\beta$  is not possible,

### 22. Solution: Correct answer is (a).

The energy of a hydrogen atom wavefunction is given by

$$\begin{split} E_n &= -\frac{13.6}{n^2} \\ \therefore E_{2s} &= -\frac{13.6}{2^2} = -\frac{13.6}{4} \quad E_{3s} = \frac{13.6}{3^2} = -\frac{13.6}{9} \\ H_{11} &= <\varphi_{2s} + \varphi_{3s}|H|\varphi_{2s} + \varphi_{3s} = -\frac{13.6}{4} - \frac{13.6}{9} \\ H_{22} &= <\varphi_{2s} - \varphi_{3s}|H|\varphi_{2s} + \varphi_{3s} = -\frac{13.6}{4} - \frac{13.6}{9} \\ H_{12} &= H_{21} = <\varphi_{2s} - \varphi_{3s}|H|\varphi_{2s} + \varphi_{3s} = -\frac{13.6}{4} - \frac{13.6}{9} \\ S_{21} &= S_{12} = <\varphi_{2s} + \varphi_{3s}|\varphi_{2s} - \varphi_{3s} = 1 - 1 = 0 \\ S_{12} &= <\varphi_{2s} + \varphi_{3s}|\varphi_{2s} + \varphi_{3s} = 1 + 1 = 2 \\ S_{22} &= <\varphi_{2s} - \varphi_{3s}|\varphi_{2s} - \varphi_{3s} = 1 + 1 = 2 \end{split}$$

$$\begin{aligned} & \begin{vmatrix} H_{11} - ES_{11} & H_{12} - ES_{12} \\ H_{21} - ES_{21} & H_{22} - ES_{22} \end{vmatrix} \\ & = \begin{vmatrix} -3.4 \left( 1 + \frac{4}{9} \right) 2 - E \times 1 & -3.4 \left( 1 - \frac{4}{9} \right) / 2 - E \times 0 \\ -3.4 \left( 1 - \frac{4}{9} \right) / 2 - E \times 0 & -3.4 \left( 1 + \frac{4}{9} \right) 2 - E \times 1 \end{vmatrix} \end{aligned}$$

$$= \begin{vmatrix} 3.4\left(1+\frac{4}{9}\right)2 - E & 3.4\left(1-\frac{4}{9}\right)/2\\ 3.4\left(1-\frac{4}{9}\right)/2 & 3.4\left(1+\frac{4}{9}\right)2 - E \end{vmatrix}$$

### 23. Solution: Correct answer is (b).

(a) 
$$\left[\hat{x}, \frac{d}{dx}\right] = x \frac{d}{dx} - \frac{d}{dx}(\hat{x}) = x \frac{d}{dx} - \left(x \frac{d}{dx} + 1\right) = -\hat{1} \neq 0$$

(b) 
$$\left[\frac{d}{dx}, \left(\frac{d^2}{dx^2} + 2\frac{d}{dx}\right)\right] = \frac{d}{dx}\left(\frac{d^2}{dx^2} + 2\frac{d}{dx}\right) - \left(\frac{d^2}{dx^2} + 2\frac{d}{dx}\right)\frac{d}{dx} = \frac{d^3}{dx^3} + 2\frac{d^2}{dx^2} - \frac{d^3}{dx^3} - 2\frac{d^2}{dx^2} = 0$$
(c)  $\left[x^2\frac{d}{dx}, \frac{d^2}{dx^2}\right] = x^2\frac{d}{dx}\frac{d^2}{dx^2} - \frac{d^2}{dx^2}\left(x^2\frac{d}{dx}\right) = x^2\frac{d^3}{dx^3} - \frac{d^2}{dx^2}$ 

(c) 
$$\left[x^2 \frac{d}{dx}, \frac{d^2}{dx^2}\right] = x^2 \frac{d}{dx} \frac{d^2}{dx^2} - \frac{d^2}{dx^2} \left(x^2 \frac{d}{dx}\right) = x^2 \frac{d^3}{dx^3} - \frac{d}{dx} \left(x^2 \frac{d^3}{dx^3} - \frac{d}{dx} \left(\frac{d^2}{dx^2} x^2\right)\right) \neq 0$$

(d) 
$$\left[x^2, \frac{d}{dx}\right] = x^2 \frac{d}{dx} - \frac{d}{dx}(x^2) = x^2 \frac{d}{dx} - 2x \neq 0$$

### 24. Solution: Correct answer is (b).

Zero point energy is given by

$$ZPE = \frac{1}{2}hv = \frac{1}{2}h \times \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} = \frac{h}{4\pi} \sqrt{\frac{k}{\mu}}$$

Given:  $k = 2293.8 N m^{-1}$ 

Reduced mass is given by

$$\mu = \frac{m_{Cl} \times m_{Cl}}{M_{Cl} + M_{Cl}} = \frac{35 \times 35}{35 + 35} = 17.5 \ amu = \frac{17.5 \times 10^{-3}}{6.022 \times 10^{23}} = 2.91 \times 10^{-26} \ kg \ mol^{-1}$$

$$\therefore ZPE = \frac{h}{4\pi} \sqrt{\frac{k}{\mu}} = \frac{6.62 \times 10^{-34}}{4 \times 3.14} \times \sqrt{\frac{2293.8}{2.91 \times 10^{-26}}} = 14.8 \times 10^{-21} J$$

### 25. **Solution:** Correct answer is (b).

For a one-dimensional box of length L, the first excited state wavefunction is fiven by

$$E_{ES} = \sqrt{\frac{2}{L}} \sin\left(\frac{2\pi x}{L}\right)$$

For a box of length L=2a, this energy will be

$$E_{ES} = \sqrt{\frac{2}{2a}} \sin\left(\frac{2\pi x}{2a}\right) = \sqrt{\frac{1}{a}} \sin\left(\frac{\pi x}{a}\right)$$

### 26. **Solution:** Correct answer is (c).

A property of the Dirac delta function  $\delta(x-m)$  is

$$\int_{-\infty}^{+\infty} f(x) \, \delta(x-m) \, dx = f(m)$$

This property also applies to any other symmetric limits, as long as the point x=m is within these limits.

$$\therefore \int_{-a}^{+a} \sin^2\left(\frac{\pi x}{a}\right) \, \delta\left(x - \frac{a}{2}\right) \, dx = \int_{-\infty}^{+\infty} \sin^2\left(\frac{\pi x}{a}\right) \, \delta\left(x - \frac{a}{2}\right) \, dx$$
$$= \sin^2\left(\frac{\pi}{a} \times \frac{a}{2}\right) = \sin\frac{\pi}{2} = 1$$

Hence, the first order energy correction to the first excited state is given by

$$\begin{split} E_{ES}^{(1)} &= \int_{-a}^{+a} \sqrt{\frac{1}{a}} \sin\left(\frac{\pi x}{a}\right) \, \delta\left(x - \frac{a}{2}\right) \, \sqrt{\frac{1}{a}} \sin\left(\frac{\pi x}{a}\right) \, dx \\ &= \frac{1}{a} \int_{-a}^{+a} \sin^2\left(\frac{\pi x}{a}\right) \, \delta\left(x - \frac{a}{2}\right) \, dx \\ &= \frac{1}{a} \times 1 = \frac{1}{a} \end{split}$$

27. Solution: Correct answer is (d).

The bonding molecular orbitals are either  $\sigma_g$  or  $\pi_u$ .

28. **Solution:** Correct answer is (c).

The energy of single electron atomic species is given by

$$E_n = -\frac{Z^2}{n^2} \times 13.6$$

If we approximate the sodium atom as a single electron in the 3s orbital (n=3) and replace the atomic number Z by the effective nuclear charge, then we can use this formula to calculate ground state energy of a sodium atom.

$$\therefore E_{GS} = -\frac{Z_{eff}^{2}}{n^{2}} \times 13.6 = -\frac{1.84^{2}}{3^{2}} \times 13.6 = 5.1 \, eV$$

29. **Solution:** Correct answer is (a).

The first order perturbation correction to the m<sup>th</sup> state is given by

$$E_m^{(1)} = \int \Psi_m^*(\phi) H_1 \Psi_m(\phi) d\phi$$

The limits of  $\phi$  are from 0 to  $2\pi$ . Hence, for the given wavefunction, the first order correction is

$$E_m^{(1)} = \int_0^{2\pi} \left(\frac{1}{\sqrt{2\pi}}\right) e^{-im\phi} \cdot P \cos\phi \cdot \left(\frac{1}{\sqrt{2\pi}}\right) e^{im\phi} d\phi$$

$$= \frac{P}{2\pi} \int_0^{2\pi} \cos\phi d\phi$$

$$= \frac{P}{2\pi} \left[\sin\phi\right]_0^{2\pi} = \frac{P}{2\pi} \left[\sin 2\pi - \sin 0\right] = \frac{P}{2\pi} \left[0 - 0\right]$$

$$= 0$$

30. Solution: Correct answer is (a).

For a one-dimensional box with infinite potential barriers, average value of linear momentum,

$$\langle \hat{p}_r \rangle = 0$$

for all energy levels.

31. Solution: Correct answer is (c).

The uncertainty in momentum is calculated as follows.

$$\begin{split} &\Delta \hat{p}_x = (\langle \hat{p}_x^2 \rangle - \langle \hat{p}_x \rangle^2)^{1/2} \\ &= \left(\frac{n^2 h^2}{4a^2} - 0^2\right)^{1/2} \quad \dots \left( \because \langle \hat{p}_x^2 \rangle = \frac{n^2 h^2}{4a^2} \text{ and } \langle \hat{p}_x \rangle = 0 \right) \\ &= \frac{nh}{2a} \end{split}$$

For the lowest energy state, n = 1.

32. Solution: Correct answer is (b).

If both electrons are found on the same atom, then the molecule will be ionic, as the charge will be concentrated on one atom only. Hence, probability that both electrons will be found on the same atom in 100 inspections is the same as the probability of the wavefunction being ionic.

$$\therefore P(\Psi = \varphi_{ionic}) = \frac{0.45^2}{0.89^2 + 0.45^2} \times 100 \approx 20$$

Hence, correct answer is (B).

33. Solution: Correct answer is (a).

The molecule with the least number of electrons is the  $H_2^+$  molecular ion, which contains only one electron.

34. Solution: Correct answer is (c).

The energy of an electron in the He atom, if inter-electron repulsion is neglected, is given by

$$E = -\frac{Z^2}{n^2} \times 0.5 \ hartrees$$

For He atom ground state, Z = 2 and n = 1.

$$\therefore E = -\frac{2^2}{1^2} \times 0.5 = -2.0 \text{ hartrees.}$$

This is the energy of one electron. Thus, the energy of both electrons of the He atom combined, is

$$E = 2 \times (-2.0) = -4.0 \ hartrees$$

Hence, correct answer is (D).

35. **Solution:** Correct answer is (a).

For a one-dimensional box,

$$E \propto \frac{1}{L^2}$$

$$\therefore \frac{dE}{dL} \propto -\frac{2}{L^3}$$

$$\therefore dE \propto \frac{2 dL}{L^3}$$

$$\therefore \frac{dE}{E} = \frac{\frac{2 dL}{L^3}}{\frac{1}{L^2}} = \frac{2 dL}{L} = \frac{2 \times 10^{-9}}{10^{-3}} = 2 \times 10^{-6}$$

$$\therefore \% \text{ change in energy} = \frac{dE}{E} \times 100 = 2 \times 10^{-4}$$

36. Solution: Correct answer is (b)

$$\left[x, \frac{d}{dx}\right] f(x) = x \frac{d}{dx} f(x) - \frac{d}{dx} (x f(x))$$

$$= x \frac{d}{dx} f(x) - \left(x \frac{d}{dx} f(x) + f(x) \frac{d}{dx} (x)\right)$$

$$= f(x)$$

37. Solution: Correct answer is (b).

The ground state energy for hydrogen atom is - 13.6 eV. The ground state energy of a harmonic oscillator is  $0.5h\nu$ . The energy of a three dimensional box is

# RADIOACTIVITY

### **Previous Year Exam Question & Solutions**

### [GATE 2004]

- The number of hyperfine split lines observed in ESR spectrum of methyl radical is
  - (a) 1

(b) 4

(c) 6

(d) 8

[GATE 2016]

- Among the following, the most stable isotope to radioactive decay is
  - (a)  $^{206}_{82}Pb$

 $(b)^{210}_{82}Pb$ 

(c)  $^{212}_{82}Pb$ 

 $(d)^{214}_{82}Pb$ 

[GATE 2020]

The fission reaction of  $^{235}_{92}U$  with thermal neutron is represented below.

$$\overset{235}{_{92}}U + \overset{1}{_{0}}n \longrightarrow \overset{236}{_{92}}U - \overset{99}{_{41}}Nb \longrightarrow X_{1} \longrightarrow X_{2} \longrightarrow X_{3}$$

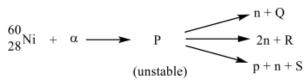
$$\overset{133}{_{51}}Sb \longrightarrow Y_{1} \longrightarrow Y_{2} \longrightarrow Y_{3} \longrightarrow Y_{4}$$

 $^{99}_{41}Nb$  and  $^{133}_{51}Sb$  are the primary fission fragment pair, which undergo series of radioactive decay to form stable nuclei  $X_3$  and  $Y_4$  (chain enders). The  $X_3$  and  $Y_4$ , respectively are:

- (a)  $^{96}_{41}Nb$  and  $^{130}_{51}Sb$  (b)  $^{99}_{44}Ru$  and  $^{133}_{55}Cs$  (c)  $^{93}_{38}Sr$  and  $^{127}_{35}Ag$  (d)  $^{87}_{35}Br$  and  $^{124}_{43}Tc$

### [GATE 2023 MSQ]

The choice(s) that correctly identify radioisotopes (P, Q, R, S) shown in the following nuclear reaction is (are)



- (a)  $P = {}^{64}_{30}Zn$
- (b)  $Q = {}^{63}_{30}Zn$
- (c)  $R = {}^{62}_{29}Cu$
- (d)  $S = {}^{62}_{29}Cu$

	Aı	nswer k	Сеу
1	2	3	4
(b)	(a)	(b)	(a),(b),(d)

### :: SOLUTIONS ::

**Solution:** Correct answer is

$$\dot{C}H_3 \Rightarrow Hypertone = (2NI + 1) = (2^*3^*1/2 + 1) = 4lines$$

Solution: Correct answer is (a)

Lead (Pb) has four stable isotopes:

<sup>204</sup>Pb, <sup>206</sup>Pb, <sup>207</sup>Pb, <sup>208</sup>Pb, <sup>204</sup>Pb, is entering a primordial nuclide and is not a radiologenic nuclide

**Solution:** Correct answer is (b)

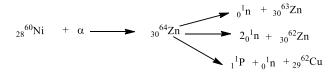
The radioactive series of fission fragment 99Nb (mass number  $A = 4 \times 24 + 3$ ) gives only those daughter nuclei (or stable end product) which have mass number A=4n+3, where n is an integer. Thus, daughter nuclei may have mass number A= 99, 95, 91, 87, 83, 79,.....etc. from the given options, 87Br and 99Ru Nuclei are the only two possibilities for stable nuclei X<sub>3</sub>. similarly, the radioactive series of fission fragment <sup>133</sup>Sb gives only those daughter nuclei (or stable end product) which have mass number A=4n+1. Where, n is an integer. Thus, daughter nuclei may have mass numbers A=133,129,125,121, etc.

From the given options, <sup>133</sup>Cs is the only possibility for stable nucleus Y

Hence, X<sub>3</sub> and Y<sub>4</sub> are <sup>99</sup>Ru and <sup>133</sup>Cs respectively.

Solution: Correct answer is (a), (b), (d)  $\alpha$ -particle ( $^{4}_{2}$ He)

> When  $\alpha$  particle emit atomic number increases by 2 and mass number increases by 4.



## **BIOINORGANIC**

### **Previous Year Exam Question & Solutions**

### [GATE 2001]

- 1. The metals involved in nitrogenase are
  - (a) Fe and Mg
- (b) Mo and K
- (c) Mo and Fe
- (d) Fe and K.

### [GATE 2003]

2. "Matching" exercises. choose the correct one from the alternatives A, B, C and D.

Column-I	Column-II
P. ZnSO4(aq)+K4	1. Enzymatic
[Fe(CN)6[aq]→Products	reaction
Q. Zn(s)+CuSO4(aq)]→Products	2. Chain reaction
R. $H2+Cl2 \xrightarrow{\Delta} Products$	3. Redox reaction
S. Fischer-Tropsch synthesis of	4. Precipitation
hydrocarbons	reaction
	5. Surface reaction
	6. Hydrolysis
	reaction

- (a) P-2, Q-4, R-5, S-6
- (b) P-1, Q-3, R-2, S-4
- (c) P-4, Q-3, R-2, S-5
- (d) P-1, Q-6, R-2, S-5

### [GATE 2004]

3. Match the following:

P: Ferritin	I electron transport
Q: Vitamin B12	II. Ionophore
R: Cytochromes	III. Oxygen transport
S: Valinomycin	IV. Nitrogen fixation
	V. Organometallic enzyme
	VI. Iron storage

- (a) P-VI, Q-IV, R-II, S-I
- (b) P-I, Q-III, R-VI, S-IV
- (c) P-III, Q-V, R-IV, S-VI
- (d) P-VI, Q-V, R-I, S-II

### [GATE 2005]

- 4. The metal present at the active site of the protein carboxypeptidase A is
  - (a) Zinc

- (b) molybdenum
- (c) magnesium
- (d) cobalt

### [GATE 2005]

5. Match the column:-

Column-I	Column-II
(P) Cytochromec	(I) Molybdenum
(Q) Calmodulin	(II) Potassium
(R) Chlorophyll	(III) Magnesium
(Q) Alcohol dehydrogenase	(IV) Zinc
	(V) Iron
	(VI) Calcium

- (a) P-V, Q-VI, R-III, Q-V
- (b) Q-II, Q-III, Q-IV, Q-VI
- (c) R-III, R-IV, R-VI, R-III
- (d) S-IV, S-V, S-II, S-IV

[GATE 2005]

- 6. Matals used in automobile catalytic converters are:
  - (a) Pt and Pd
- (b) Pt and Rh
- (c) Pd and Rh
- (d) Rh and Ni

[GATE 2005]

7. **Statement**: D-Glucose and D-mannose give the same phenylosazone.

**Reason:** Osazone formation results in a loss of the stereocentre at C2 but does not affect other stereo centers.

Assertion: D-Glucose and D-mannose are enantiomers.

- (a) Both Reason and Assertion are correct
- (b) Both Reason and Assertion are wrong.
- (c) Reason is correct but Assertion is wrong.
- (d) Reason is wrong but Assertion is correct.

[GATE 2006]

- 8. Iron-sulphur clusters in biological systems are involved in
  - (a) proton transfer
- (b) atom transfer
- (c) group transfer
- (d) electron transfer

[GATE 2006]

- 9. The amino acid side chain high affinity for Ca2+ and Cu2+ in metallo-proteins is:
  - (a) carboxylate in both the cases.
  - (b) imidazole in both the cases.
  - (c) caboxylatefor Ca2+ and imidazole for Cu2+.
  - (d) imidazole for Ca2+ and carboxylate for Cu2+.

[GATE 2006]

- 10. In biological systems, the metal ion involved in the dioxygen transport besides Fe is
  - (a) Co

(b) Zn

(c) Mg

(d) Cu

[GATE 2007]

- 11. In photosynthesis, the predominant metal present in the reaction centre of photosystem II is
  - (a) Zn

(b) Cu

(c) Mn

(d) Fe

[GATE 2007]

- 12. Zn in carbonic anhydrase is coordinated by three histidine and one water molecule. The reaction of CO2 with this enzyme is an example of
  - (a) electrophilic addition
  - (b) electron transfer
  - (c) nucleophilic addition
  - (d) electrophilic substitution

### [GATE 2007]

- 13. The catalyst used in the conversion of ethylene to acetaldehyde using Wacker process is
  - (a) HCo(CO)4
  - (b) [PdCl4]2-
  - (c) V2O5
  - (d) TiCl4 in the presence of Al(C2H5)3

### [GATE 2008]

- 14. In biological systems, the metal ions involved in electron transport are
  - (a) Na+ and K+
- (b) Zn2+ and Mg2+
- (c) Ca2+ and Mg2+
- (d) Cu2+ and Fe3+

### [GATE 2009]

- 15. In the transformation of oxy-haemoglobin to deoxyhaemoglobin
  - (a) Fe2+ in the low spin state changes to Fe2+ in the high spin state
  - (b) Fe2+ in the low spin state changes to Fe3+ in the low spin state
  - (c) Fe2+ in the high spin state changes to Fe2+ in the low spin state
  - (d) Fe2+ in the high spin state changes to Fe3+ in the high spin state

### [GATE 2009]

- 16. Among 1he following pair of metal ions present in Nature. The first one functions as an Electron transfer agent and the second one catalyzes the hydrolysis reactions. The correct pair is
  - (a) Fe and Zn
- (b) Mg and Fe
- (c) Co and Mo
- (d) Ca and Cu

### [GATE 2011]

- 17. A well-known naturally occurring organometallic compound is
  - (a) vitamin B12 coenzyme
- (b) chlorophyll
- (c) cytochrome P-450
- (d) myoglobin

### [GATE 2011]

- 18. The red color of oxy-haemoglobin is mainly due to the
  - (a) d-d transition
  - (b) metal to ligand charge transfer transition
  - (c) ligand to metal charge transfer transition
  - (d) intraligan  $d\pi$ - $\pi$ \* transition

### [GATE 2012]

- 19. Haemoglobin is an oxygen carrying protein. The correct statement about oxy-hemoglobin is that
  - (a) the metal is low-spin in +3 oxidation state while dioxygen is in O2–form
  - (b) the metal is high-spin in +3 oxidation state while dioxygen is in O2–form
  - (c) the metal is low-spin in +3 oxidation state while dioxygen is in neutral form
  - (d) the metal is high-spin in +3 oxidation state while dioxygen is in neutral form

### [GATE 2013]

- 20. Oxymyoglobin Mb(O2) and oxy-haemoglobin Hb(O2)4, respectively, are
  - (a) paramagnetic and paramagnetic
  - (b) diamagnetic and diamagnetic
  - (c) paramagnetic and diamagnetic
  - (d) diamagnetic and paramagnetic

### [GATE 2014]

- 21.  $Mg^{2+}$  is preferred in photosynthesis by chlorophyll because
  - (a) it has strong spin-orbit coupling
  - (b) it has weak spin-orbit coupling
  - (c) it is a heavy metal
  - (d) it binds strongly with chlorophyll

### [GATE 2014]

22. In Monosanto acetic acid process shown below, the role of HI is

$$CH_3OH + CO \xrightarrow{Rh(I)catalyst/HI} CH_3CO_2H$$

- (a) to covert  $CH_3OH$  to a stronger nucleophile  $(CH_3O^-)$
- (b) to reduce the Rh(I) catalyst to a Rh(0) species
- (c) to reduce a Rh(III) active species to a Rh(I) species in the catalytic cycle
- (d) to convert  $CH_3OH$  to  $CH_3I$

### [GATE 2015]

- 23. Among the given pH values, the O2 binding efficiency of hemoglobin is maximum at
  - (a) 6.8

(b) 7.0

(c) 7.2

(d) 7.4

### [GATE 2015]

- 24. Identify the function of hemocyanin and the metal responsible for it.
  - (a) O2 transport and Fe
  - (b) O2 transport and Cu
  - (c) electron transport and Fe
  - (d) electron transport and Cu

### [GATE 2016]

- 25. During oxygen transport by hemerythrin, oxygen is bound as
  - (a) O2- to one Fe(III) only
  - (b) HO2-to one Fe(III) only
  - (c) O22-to one Fe(II) and one Fe(III)
  - (d) O22-to two Fe(II)

### [GATE 2016]

- 26. At pH 7.2 and 10 Torr oxygen partial pressure, the extent of O2 binding is
  - (a) high for both haemoglobin and myoglobin
  - (b) high for haemoglobin and low for myoglobin
  - (c) high for myoglobin and low for haemoglobin
  - (d) low for both haemoglobin and myoglobin

				ANS	WER I	<b>KEY</b>					
1	2	3	4	5	6	7		8	9		10
(c)	(c)	(d)	(a)	(d)	(a)	(a)		(d)	(c	)	(d)
11	12	13	14	15	16	17		18	19	)	20
(c)	(c)	(b)	(d)	(a)	(a)	(a)		(d)	(a	)	(b)
21	22	23	24	25	26	27		28	29	•	30
(b)	(d)	(d)	(b)	(b)	(c)	(a)		(c)	(a	)	(b)
31	32	33	34	35	36	37		38			
(c)	(b)	(c)	(b)	(a),(d)	(d)	(b),(d	<b>:</b> )	(a)(b)	(d)		

### :: SOLUTIONS ::

### 1. Solution: Correct answer is (c)

The metals involved in nitrogenase are Mo and Fe Nitrogenase is an enzyme complex responsible for nitrogen fixation, which converts atmospheric nitrogen (N<sub>2</sub>) into ammonia (NH<sub>3</sub>). It contains two important metal-containing components: one with **molybdenum (Mo)** and the other with **iron (Fe)**. These metals play a crucial role in the enzyme's activity.

### **2. Solution:** Correct answer is (c)

- (P) ZnSO4 (aq)+K4 [Fe(CN)6](aq)  $\rightarrow$  K2SO4+ Zn<sub>2</sub> [Fe(CN),] Precipitation reaction
- (Q)  $Zn(s)+CuSO4(aq) \rightarrow ZnSO4 + Cu(s)$ Redox reaction
- (R)  $H_2+Cl_2HCI$  (chain reaction due to formation of free radical)
- (S) Fischer tropsch synthesis of hydrocarbons → it involve conversion of CO and H2 into liquid hydrocarbon. The reaction occurs in presence of certain metal catalyst which provides surface for reaction. Hence, it is a surface reaction.

### **3. Solution:** Correct answer is (d)

### Ferritin: Iron storage

Ferritin is a protein complex that stores iron in a bioavailable form in cells. It helps regulate iron homeostasis in the body.

### - Vitamin B12: Organometallic enzyme

Vitamin B12 (cobalamin) contains a cobalt ion in its structure and acts as a coenzyme in various biochemical reactions, including DNA synthesis and fatty acid metabolism. It is considered an organometallic compound because of the metal-carbon bond in its structure.

### Cytochromes: Electron transport

Cytochromes are heme-containing proteins that play a critical role in electron transport chains, particularly in mitochondria during cellular respiration, facilitating the transfer of electrons.

### - Valinomycin: Ionophore

Valinomycin is a cyclic molecule that acts as an ionophore, facilitating the transport of potassium ions ( $K^+$ ) across biological membranes.

Ferritin → Iron storage

Vitamin B12 → Organometallic enzyme

Cytochromes → Electron transport

Valinomycin → Ionophormoduloas

### 4. Solution: Correct answer is (a)

The metal present at the active site of the protein carboxypeptidase A is zinc

Carboxypeptidase A is a metalloprotease enzyme that uses a zinc ion at its active site to catalyze the hydrolysis of peptide bonds at the carboxyl end of proteins and peptides. The zinc ion plays a crucial role in the enzyme's catalytic mechanism.

### **5. Solution:** Correct answer is (d)

### - Cytochrome-C → Iron

Cytochrome C contains heme groups, where the iron (Fe) in the heme is crucial for its electron transfer function in the electron transport chain.

### Calmodulin → Calcium

Calmodulin is a calcium-binding messenger protein. It undergoes conformational changes upon binding to calcium ions, allowing it to regulate various enzymes and cellular processes.

### - Chlorophyll → Magnesium

Chlorophyll, the green pigment in plants responsible for photosynthesis, contains a magnesium ion (Mg<sup>2+</sup>) at its center. This metal ion is essential for the molecule's ability to absorb light and convert it into chemical energy.

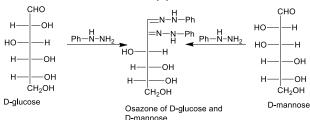
### - Alcohol Dehydrogenase → Zinc

Alcohol dehydrogenase (ADH) is an enzyme that contains zinc ions at its active site, which are critical for its catalytic activity in the conversion of alcohols to aldehydes or ketones.

### **6. Solution:** Correct answer is (a)

Pd and Rh are two precious metal that is used in autocatalytic convertor.

### **7. Solution:** Correct answer is (a)



During Osazone formation stereocentre of C, is lost. Dglucose and D-mannose are distereomers

### 8. Solution: Correct answer is (d)

Iron sulphur cluster in biological systems are involved in electron transfer reaction.

These clusters consist of iron (Fe) and sulfur (S) atoms and play a crucial role in electron transfer processes, particularly in the electron transport chain and various redox reactions within cells. The iron-sulfur clusters facilitate the movement of electrons by undergoing reversible oxidation and reduction. They are key components in enzymes and proteins involved in cellular energy production, such as in the mitochondria and photosynthesis.

### **9. Solution:** Correct answer is (c)

Carboxylate for Ca<sup>2+</sup> and imidazole for Cu<sup>2+</sup>.

### 10. Solution: Correct answer is (d)

In biological systems, the Cu involved in the dioxygen transport besides Fe

Copper plays a role in dioxygen transport and binding in certain proteins, such as **hemocyanin**, which is an oxygencarrying molecule found in some arthropods and mollusks. Unlike hemoglobin (which contains iron), hemocyanin uses copper ions to bind oxygen.

### **11. Solution:** Correct answer is (c)

In photosynthesis, Mn is the predominant metal present in the reaction centre of photosystem-11.

Manganese is a crucial component of the oxygen-evolving complex (OEC) in photosystem II, where it plays a key role in the splitting of water molecules to release oxygen during the light-dependent reactions of photosynthesis.

### **12. Solution:** Correct answer is (c)

Zn in carbonic anhydrase, the  $CO_2$  undergoes nucleophilic addition reaction.

In carbonic anhydrase, the zinc ion  $(Zn^{2+})$  at the active site facilitates the conversion of carbon dioxide  $(CO_2)$  into bicarbonate  $(HCO_3^-)$  by coordinating with a water molecule. The water molecule becomes deprotonated, and the hydroxide ion  $(OH^-)$  formed acts as a nucleophile, attacking the electrophilic carbon of  $CO_2$ , leading to the formation of bicarbonate.

### **13. Solution:** Correct answer is (b)

Wacker's process

$$\begin{split} &C_2H_4 + H_2O + [PdCl_4]^{-2} \to CH_3CHO + Pd + \ 2HCl + \\ &2CI^- \\ &Pd + 2CuCl_2 + 2Cl \to [Pd(Cl_4)]^{-2} + 2CuCl \end{split}$$

Net reaction 
$$C_2H_4 + \frac{1}{2}O_2 \rightarrow CH_3CHO$$

 $2CuCl + \frac{1}{2}O_2 + 2HCI \rightarrow 2CuCl_2 + H_2O$ 

### **14. Solution:** Correct answer is (d)

In biological systems,  $Cu^{2+}$  and  $Fe^{2+}$  metal ion involve in electron transport. This is due their variable oxidation state.

Both copper (Cu) and iron (Fe) play crucial roles in electron transport. Copper is involved in proteins like cytochrome c oxidase, while iron is part of iron-sulfur clusters and heme groups in cytochromes, which are essential components of the electron transport chain, particularly in mitochondria and chloroplasts.

### **15. Solution:** Correct answer is (a)

The transformation of oxyhaemoglobin to deoxyhaemoglobin  $Fe^{2+}$  involves change in low spin state to high spin state.

In deoxyhaemoglobin,  $Fe^{2+}$  is in high spin state.

In oxyhaemoglobin, iron of heme group bind with oxygen molecule, and Fe become low spin

### **16. Solution:** Correct answer is (a)

Fe act as electron transfer agent in many reaction. Zn act as catalyst in hydrolysis reaction specially enzymatic reaction by carboxypeptidase.

### 17. Solution: Correct option (a)

Vitamin  $B_{12}$  co-enzyme is a naturally occurring organometallic compound.

### **18. Solution:** Correct answer is (d)

Red colour of oxyhemoglobin is mainly due to  $\pi-\pi^*$  transition in porphyrin system.

The red color of **oxyhemoglobin** is primarily due to the electronic transitions involving the iron ion in the heme group. In particular, the iron undergoes a **d-d transition** in which electrons in the d-orbitals of the iron ion move between different energy levels, absorbing light in the visible spectrum. This absorption contributes to the red color observed in oxygen-bound hemoglobin.

### **19. Solution:** Correct answer is (a)

In oxyhaemoglobin the metal is low-spin in +3 oxidation state while dioxygen is in O.

### **20. Solution:** Correct answer is (b)

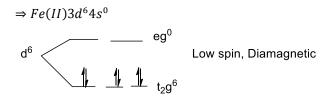
Oxymyoglobin Mb(O2)

 $\Rightarrow Fe(II)3d^64s^0$ 



Oxyhemoglobin Hb(O2)4

Low spin, Diamagnetic



### 21. Solution: Correct answer is (b)

In photosynthesis,  $Mg^{2+}$  is preferred and it is present in chlorophyll. It has small spin-orbit coupling. So, inter system crossing is inhibited which favours the energy transfer from the excited singlet state.

### 22. Solution: Correct answer is (d)

In Monsanto acetic acid process role of HI is to convert  $CH_3OH$  to  $CH_3I$   $CH_3OH + HI \rightarrow CH_3I + H_2O$ 

### 23. Solution: Correct answer is (d)

The  ${\cal O}_2$  binding efficiency of hemoglobin is maximum at blood pH is 7.4

### **24. Solution:** Correct answer is (b)

hemocyanin is a copper containing protein which is responsible for oxygen transport in some invertebrates

### **25. Solution:** Correct answer is (b)

During oxygen transport by hemerythrin, oxygen is bound as  $HO_2^-$  to one Fe(III) only

### **26. Solution:** Correct answer is (c)

At low pH and low pressure Hb has less oxygen binding tendency. While for Mb this is hight.

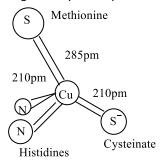
### **27. Solution:** Correct answer is (a)

Chlorophylls are complexes of  $Mg^{2+}$  with porphyrin ring in which one of the pyrrole rings has been reduced. A porphyrin ring with one double bond reduced is called a chlorin. Therefore, chlorophylls are the complexes of  $Mg^{2+}$  metal ion with substituted chlorin (macrocyclic skeleton).

### 28. Solution: Correct answer is (c)

Plastocyanin is important bioinorganic complex, they help in electron transfer during photosynthesis. They are present between Photosystem I and Photosystem II. It changes oxidation state from +1 to +2 or vice versa during electron transfer. The oxidised form of copper contain the active site Cu+2 ions, thus the copper ion forms a trigonal pyramidal and tetrahedral structure with methionine, Cysteine, and two histidine residues, here the copper ion

is forming a structure that is distorted and tetrahedral because of the geometry of the protein.



### 29. Solution: Correct answer is (a)

Oxy-myoglobin is formed when myoglobin which is globular protein binds with it. Oxy-myoglobin store oxygen in muscles. So, oxygen is present in O2- which is superoxide ion state in oxy-myoglobin. Oxy-hemocyanin is formed by the oxygenation of hemocyanin. Hemocyanin is a protein that contains copper and is generally found in crustaceans. Oxy-hemocyanin is blue in colour and used for binding and storage of oxygen. O22- which is peroxide ion in Oxyhemocyanin.

### **30. Solution:** Correct answer is (b)

Ferritin metal storage
Rubredoxin electron transfer
Cobalamin methyl transfer
Carbonic anhydrase acid-base catalysis

### Ferritin → Metal storage

Ferritin is a protein that stores iron in a non-toxic, bioavailable form, helping regulate iron levels in the body.

### Rubredoxin → Electron transfer

Rubredoxin is a small iron-containing protein involved in electron transfer reactions, typically in anaerobic microorganisms.

### Cobalamin → Methyl transfer

Cobalamin (Vitamin B12) acts as a coenzyme in methyl transfer reactions, important for DNA synthesis and metabolism.

### - Carbonic anhydrase → Acid-base catalysis

Carbonic anhydrase is an enzyme that catalyzes the reversible conversion of carbon dioxide and water to bicarbonate and protons, playing a role in regulating pH and  $CO_2$  levels.

### 31. Solution: Correct answer is (c)

